

Finding Inverses of Exponentials

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- 1.) Find the inverse of $y = 4^x$
switch x and y

write as log

"Log it off"

$$x = 4^y$$

$$\log_4 x = \log_4 4^y$$

$$\log_4 x = y$$

- 2.) Find the inverse of $y = 8^x$

switch x and y

write as log

"Log it off"

$$x = 8^y$$

$$\log_8 x = \log_8 8^y$$

$$\log_8 x = y$$

- 3.) Find the inverse of $y = 3 + 2^x$

switch x and y

isolate exponential term

write as log

"Log it off"
solve for y

$$x = 3 + 2^y$$

$$x - 3 = 2^y$$

$$\log_2 (x - 3) \log_2 2^y$$

$$\log_2 (x - 3) = y$$

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Finding Inverses of Logs

1) Find the inverse of $y = \log_7 x$

switch x and y

write as exponent

"Exponentiate"

$$x = \log_7 y$$

$$7^x = 7^{\log_7 y}$$

$$7^x = y$$

Common
log
base 10

2) Find the inverse of $y = \log(x - 2)$

switch x and y

write as exponent

"Exponentiate"

solve for y

$$x = \log(y - 2)$$

$$10^x = 10^{\log(y - 2)}$$

$$10^x = y - 2$$

$$10^x + 2 = y$$

3.) Find the inverse of $y = 5 + \log x$

switch x and y

isolate log term

write as exponent

solve for y

$$x = 5 + \log y$$

$$x - 5 = \log y$$

$$10^{x-5} = 10^{\log y}$$

$$10^{x-5} = y$$